



Incorporating Episodic Vertical Displacements into Vertical Reference Frames

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- Examples from New Zealand earthquakes throughout
- Types of vertical deformation
- Impact on global and local reference frames
- Measuring vertical deformation
- Modelling vertical deformation
- Using a vertical deformation model



1. Types of Vertical Deformation

Continuous Vertical Deformation

- Until recently, vertical signal often difficult to detect (GNSS noisier in vertical)
- Secular vertical deformation
- Non-secular vertical deformation
 - Post-seismic decay
 - Natural subsidence
 - Human-induced subsidence (resource extraction)
 - Slow landslides
 - Slow earthquakes



Episodic Vertical Deformation

- Earthquakes the major natural cause
- Landslides
- Subsidence



New Zealand Examples

| Name | Date | Magnitude | Max Vt (m) |
|------------------------------|-------------|-----------|------------|
| Secretary Island (Fiordland) | 22 Aug 2003 | 7.2 | 0.72 |
| Macquarie Island | 24 Dec 2004 | 8.1 | 0.005 |
| George Sound (Fiordland) | 16 Oct 2007 | 6.7 | 0.27 |
| Dusky Sound | 15 Jul 2009 | 7.8 | 0.39 |
| Darfield | 4 Sep 2010 | 7.1 | 1.75 |
| Christchurch | 22 Feb 2011 | 6.3 | 0.48 |
| Christchurch | 13 Jun 2011 | 6.3 | 0.13 |
| Christchurch | 23 Dec 2011 | 6.0 | 0.36 |
| Cook Strait | 21 Jul 2013 | 6.0 | 0.024 |
| Lake Grassmere | 16 Aug 2013 | 6.6 | 0.26 |



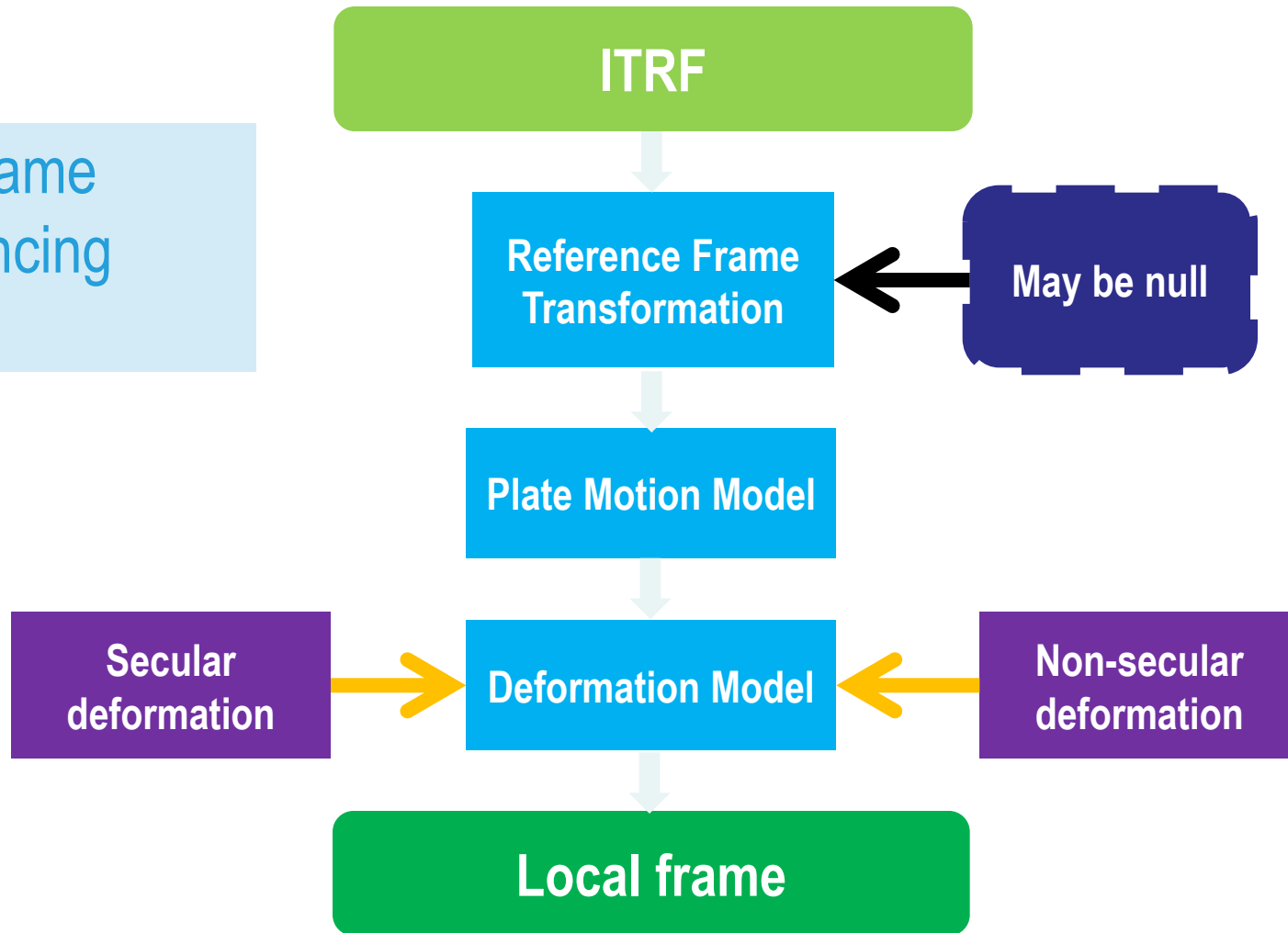


2. Impact on Global and Local Vertical Reference Frames

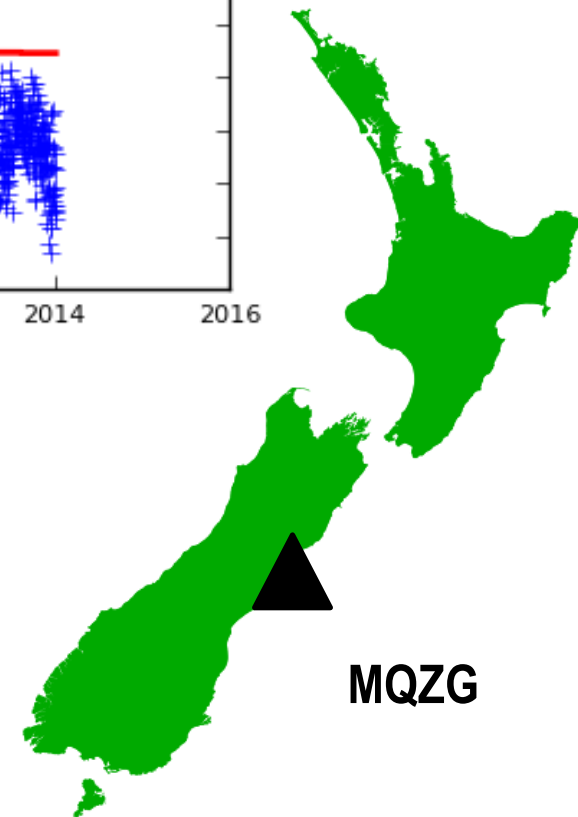
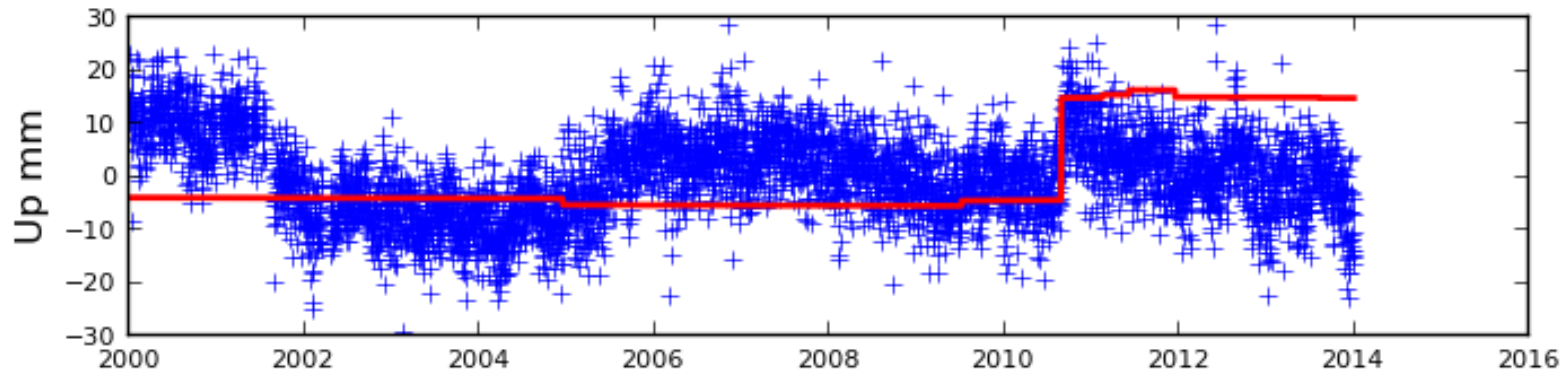
Global vs Local Frame

| Global (eg ITRF) | Local (eg NZGD2000) |
|--|--|
| Driven by global science requirements | Driven by national spatial community requirements |
| Time-varying coordinates for ground-fixed marks | Time-invariant coordinates for ground-fixed marks |
| Plate motion and/or deformation models to propagate coordinates between epochs | Plate motion and/or deformation models to generate reference coordinates |
| Native system for modern positioning techniques (GNSS) | Modern positioning techniques (GNSS) require transformation to local frame |

Two-Frame
Referencing
System



Deformation Model for ITRF Coordinate Propagation



- Little overall impact on global frame
 - Requires offset at ITRF station
- ITRF coordinates change due to episodic deformation, but this change is often less significant than a short period of continuous deformation

Impact on Local Reference Frame

- Relative accuracy of local frame is compromised
- Fluids may no longer flow from a greater height to a lesser height





User Requirements for Vertical Deformation Modelling in a Local Frame

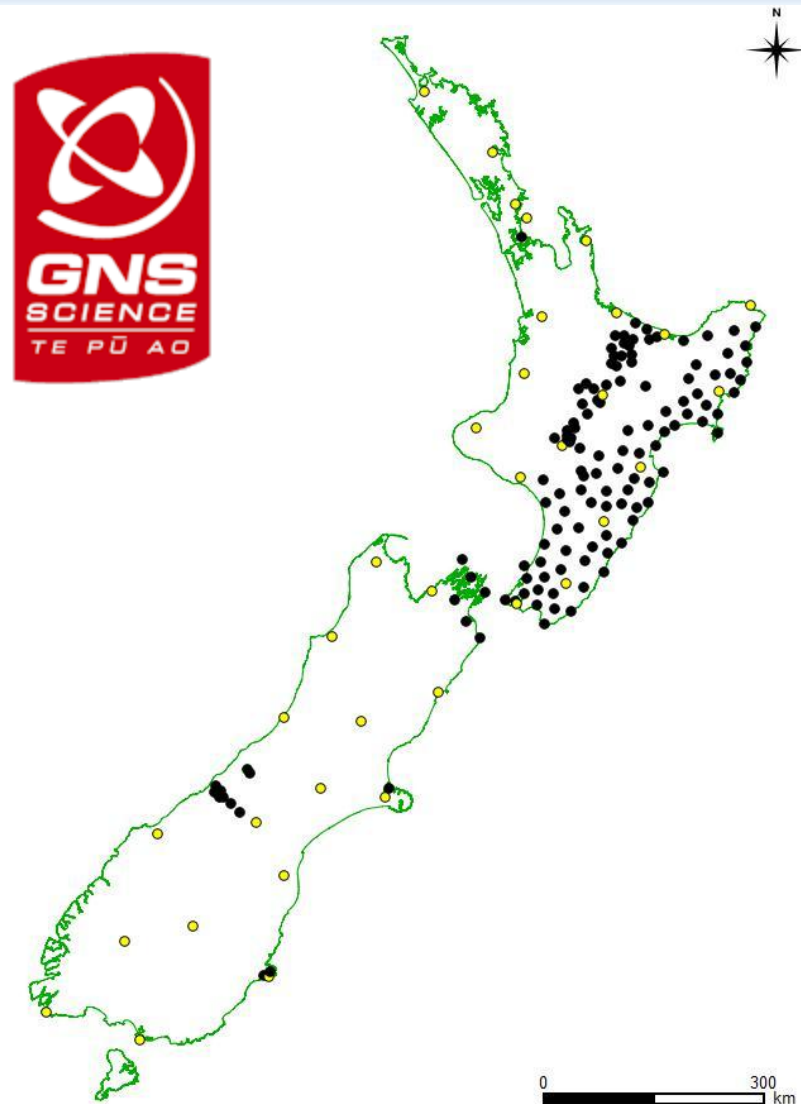
- Heights need to reflect fluid flow
- Maintain relative accuracy, especially over short distances
- Often want coordinates to reflect “local” vertical deformation, but the definition of “local” is application-dependent. Models can hide vertical deformation, which can be dangerous. Care is required!
- Generally don’t want coordinates changing for consistent vertical deformation over large areas



3. Measuring Vertical Deformation

CORS

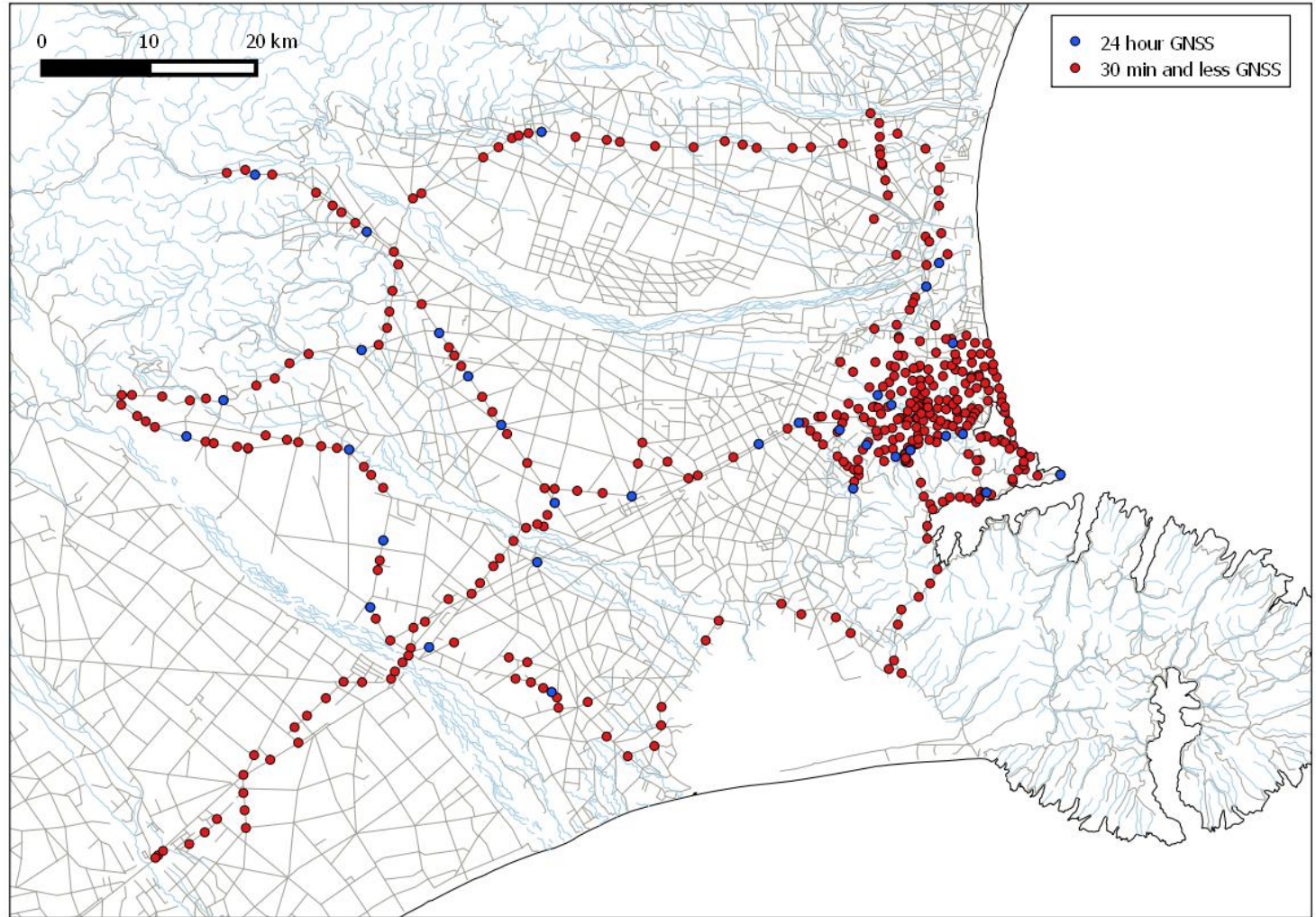
- Updated heights computed very soon after an event
- Other data uses these updated heights as control



GNSS Campaigns and Levelling



Levelling

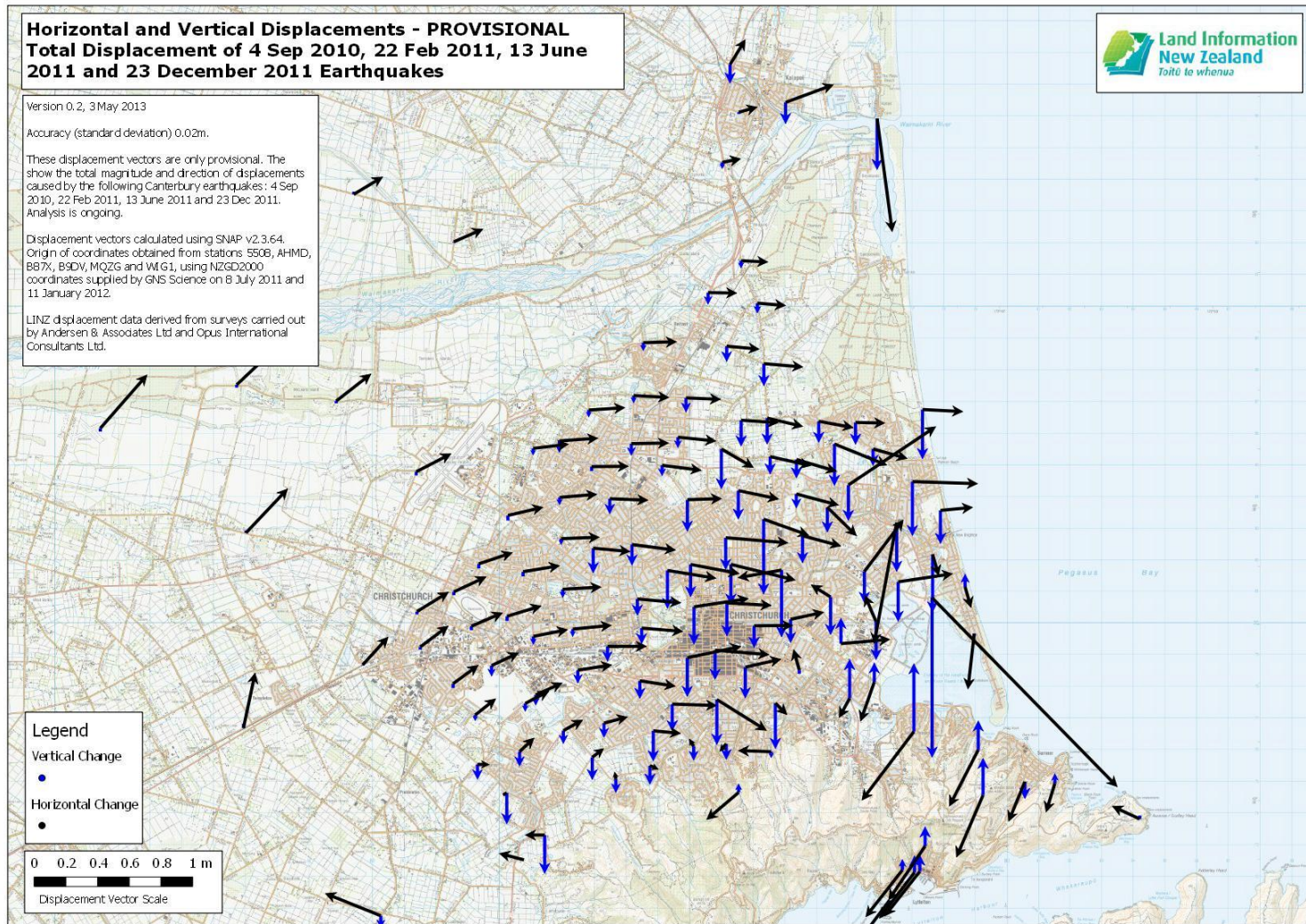
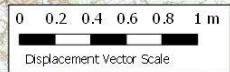


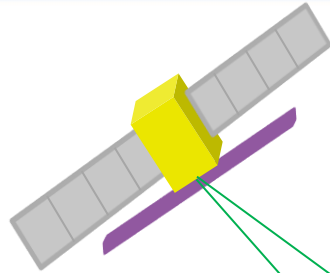
GNSS

Horizontal and Vertical Displacements - PROVISIONAL Total Displacement of 4 Sep 2010, 22 Feb 2011, 13 June 2011 and 23 December 2011 Earthquakes

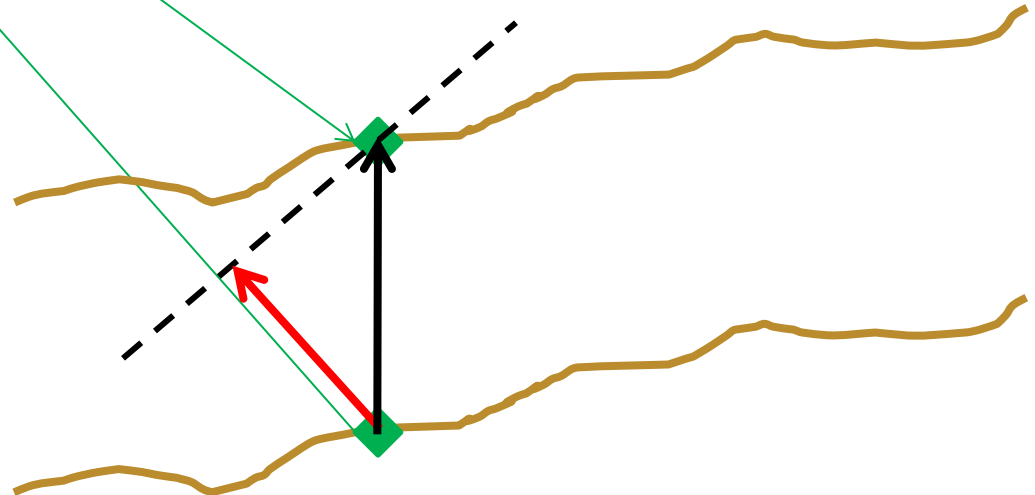
Version 0.2, 3 May 2013
 Accuracy (standard deviation) 0.02m.
 These displacement vectors are only provisional. They show the total magnitude and direction of displacements caused by the following Canterbury earthquakes: 4 Sep 2010, 22 Feb 2011, 13 June 2011 and 23 Dec 2011. Analysis is ongoing.
 Displacement vectors calculated using SNAP v2.3.64. Origin of coordinates obtained from stations 550B, AHMD, B87X, B9DV, MQZG and WIG1, using NZGD2000 coordinates supplied by GNS Science on 8 July 2011 and 11 January 2012.
 LINZ displacement data derived from surveys carried out by Andersen & Associates Ltd and Opus International Consultants Ltd.

Legend
 Vertical Change
 •
 Horizontal Change
 •

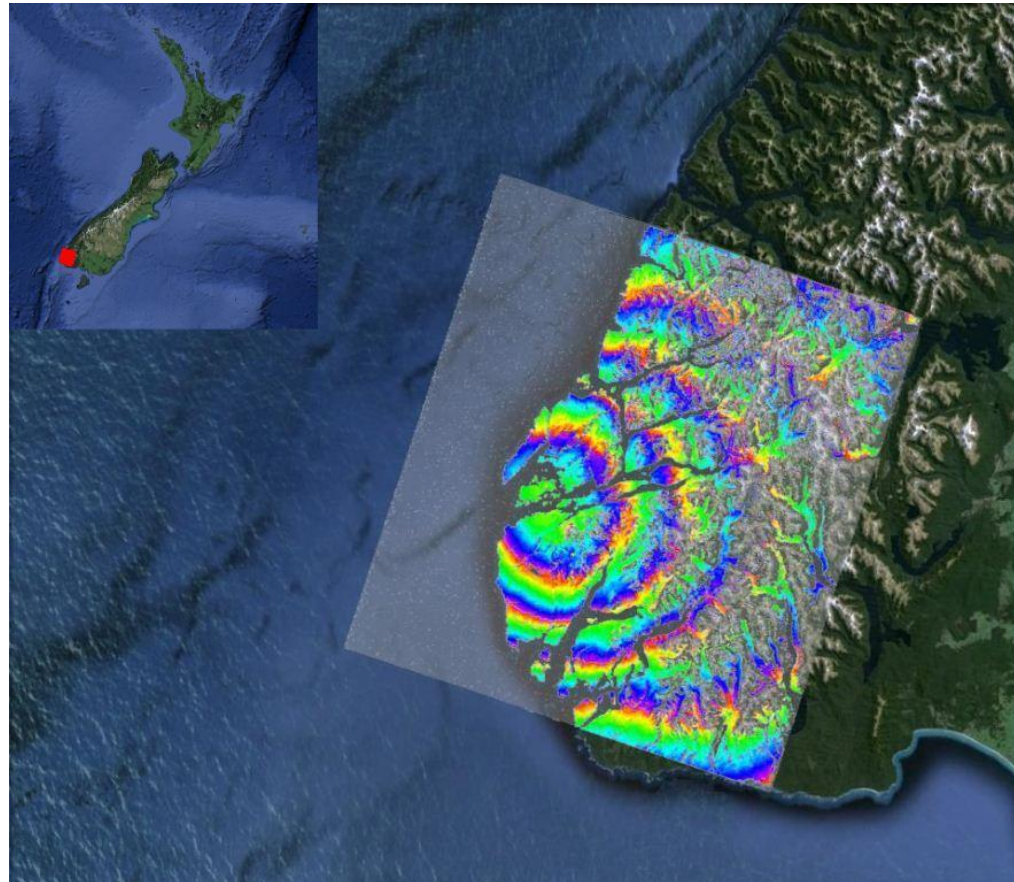




DInSAR –
Millimetre-
accurate
Deformation



DInSAR Example





Multiple Measurement Techniques

| Technique | Nominal Precision | Contribution to Geodetic System Re-establishment |
|---|-------------------|---|
| Continuously Operating Reference Stations | 0.001 – 0.010 m | Immediate indications of co-seismic displacement, monitoring of post-seismic and inter-seismic deformation. Provide the framework for all other GNSS surveys. |
| Static GNSS | 0.005 – 0.010 m | Contributes to earthquake deformation models. Provides framework for rapid static surveys |
| Rapid Static GNSS | 0.010 – 0.020 m | Provides the densest level of control to support other surveys. Contributes to earthquake deformation models |



Multiple Measurement Techniques

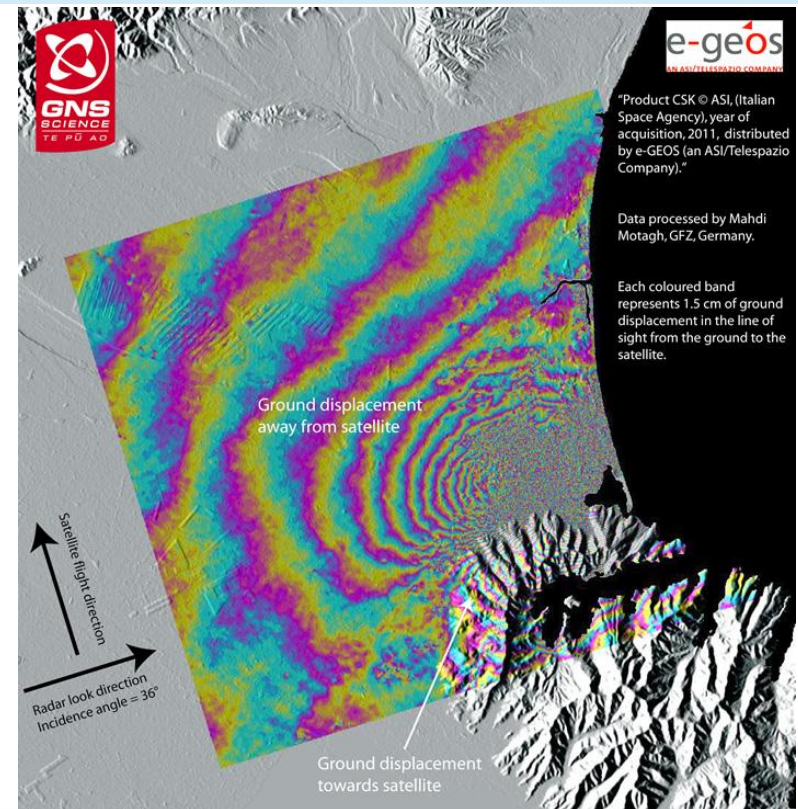
| Technique | Nominal Precision | Contribution to Geodetic System Re-establishment |
|------------------|--------------------------|---|
| InSAR | 0.010 – 0.050 m relative | Contributes to earthquake deformation model |
| Airborne LIDAR | 0.1 – 0.3 m vertical | Detailed model of height changes across the city, to assist flood control; also used to map large horizontal changes due to ground failure, using sub-pixel correlation |
| Precise Leveling | 0.001 – 0.010 m vertical | Precise orthometric height control, required for accurate design of gravity-reliant engineering schemes (e.g., |



4. Modelling Vertical Deformation

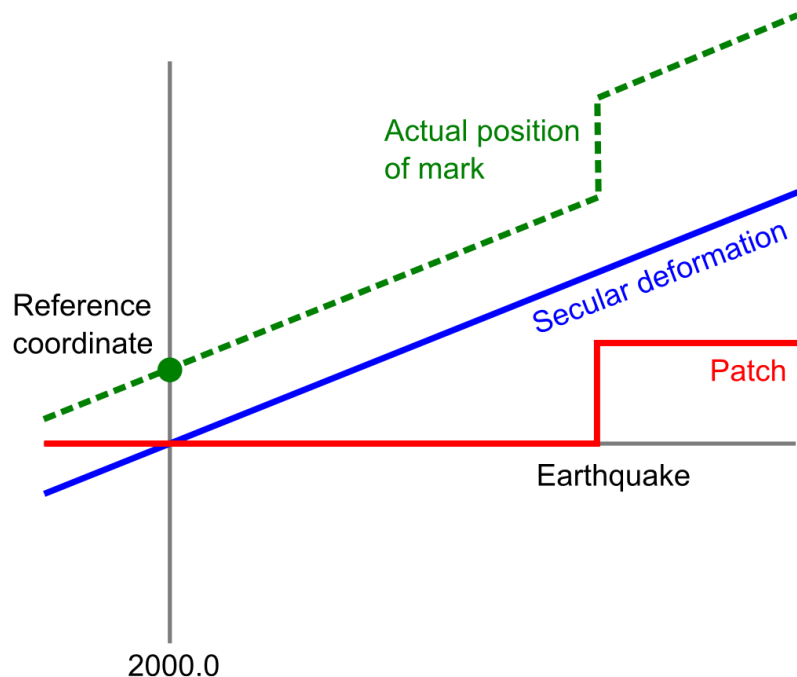
Modelling Deformation

- GNSS data provides three-dimensional displacements at surveyed points
- InSAR provides displacements in the direction of line of sight between the satellite and ground with a resolution of tens of meters
- Inversion software is used in a two-step process to estimate parameters for location and geometry of the fault plane(s), and magnitude and direction of slip

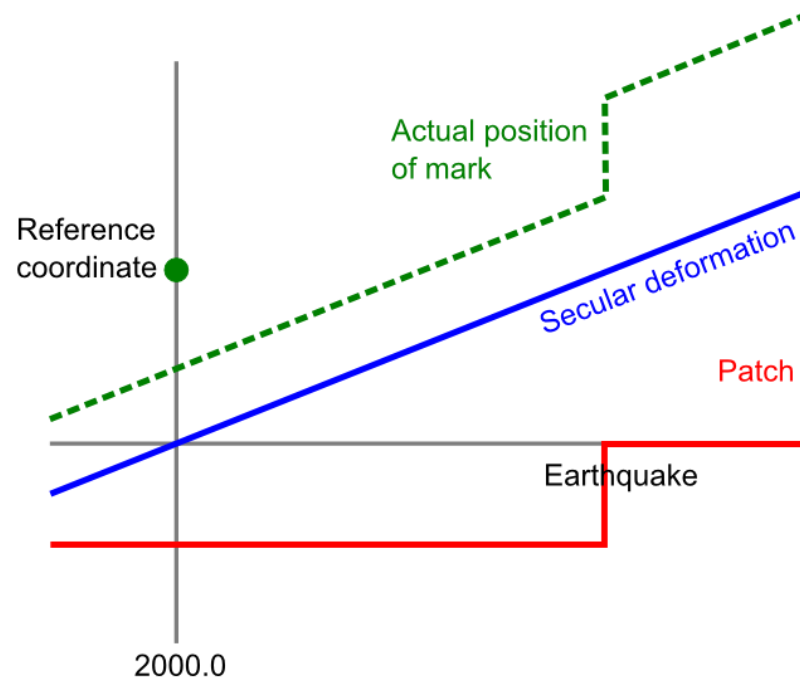


Deformation Model Patches

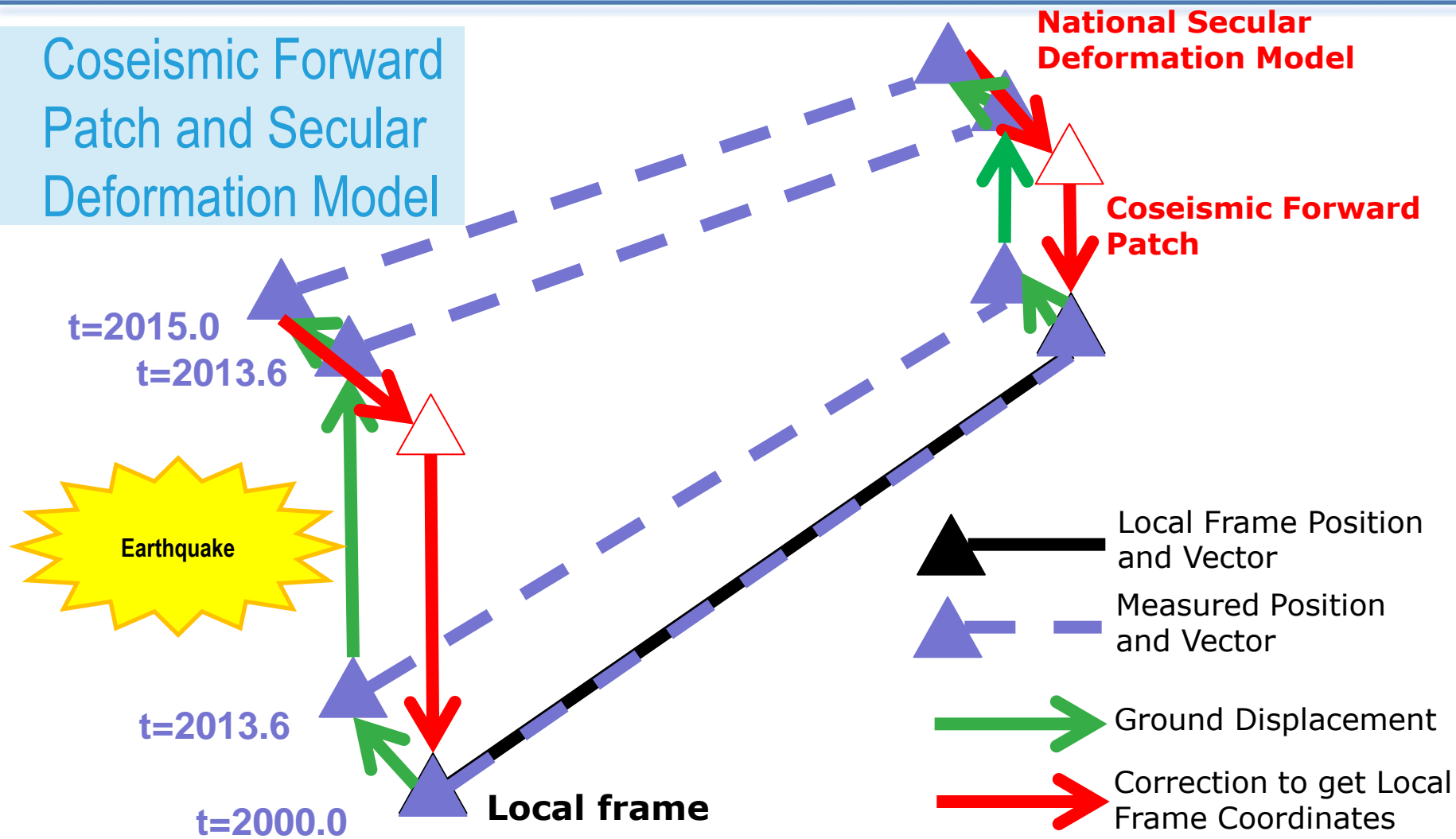
"Forward" patch



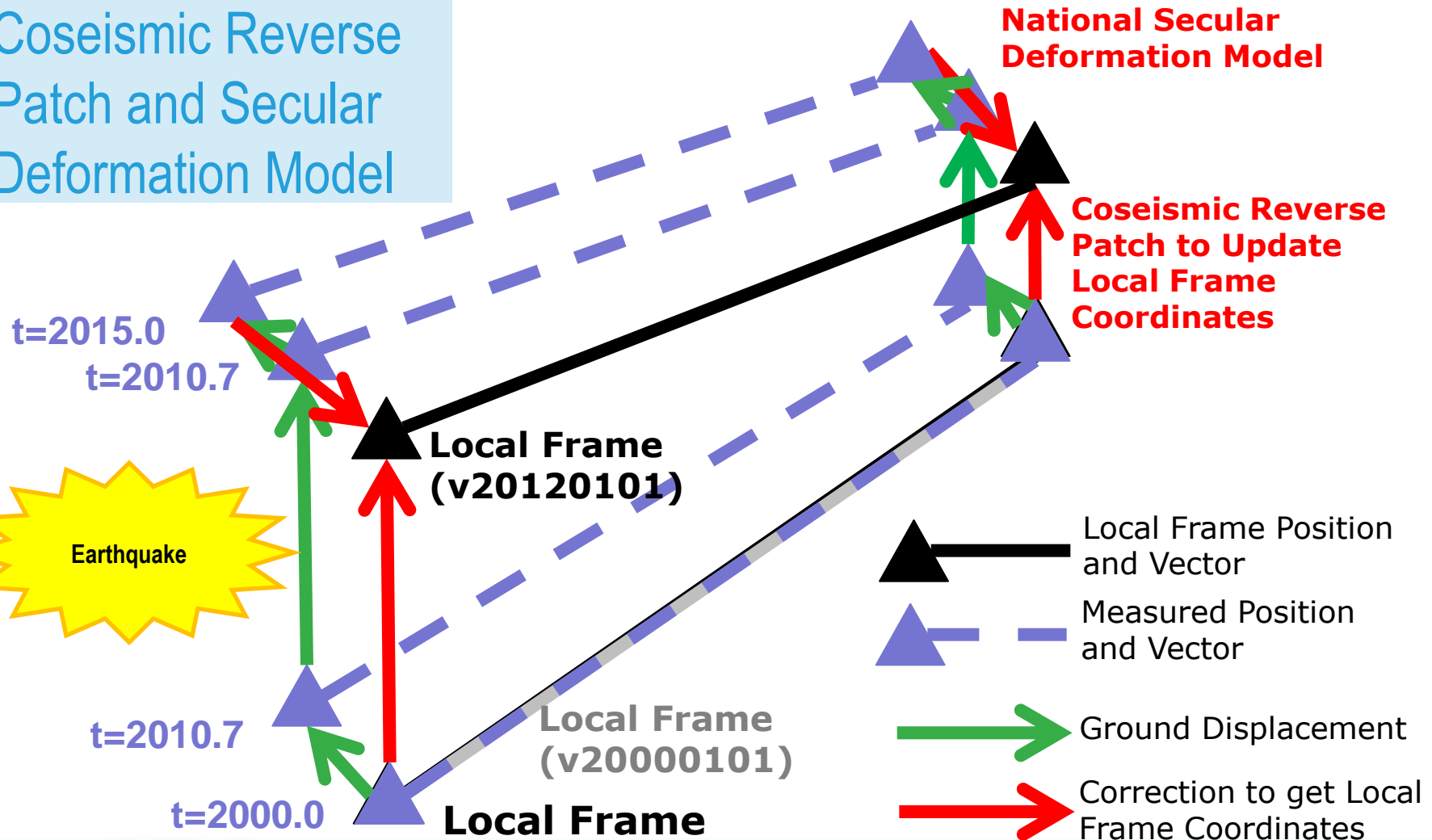
"Reverse" patch



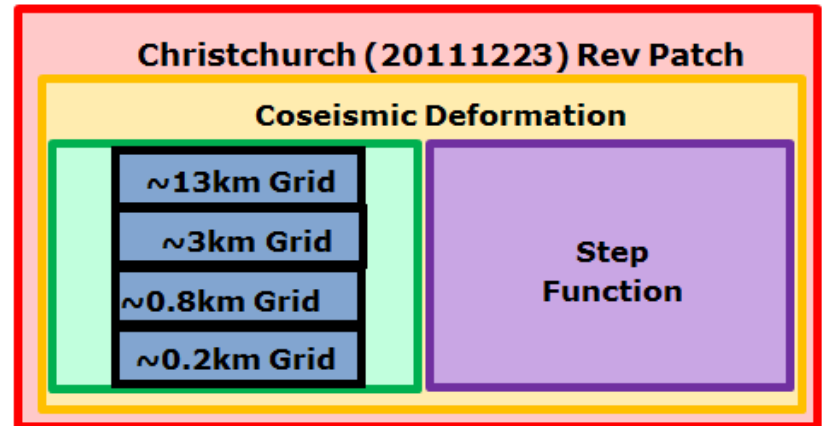
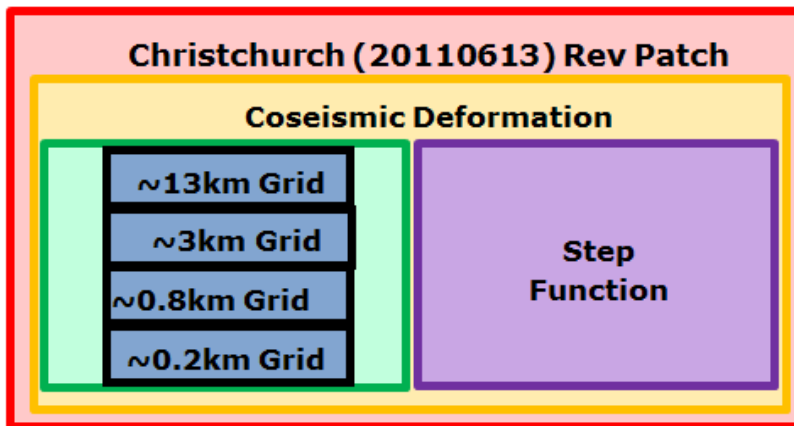
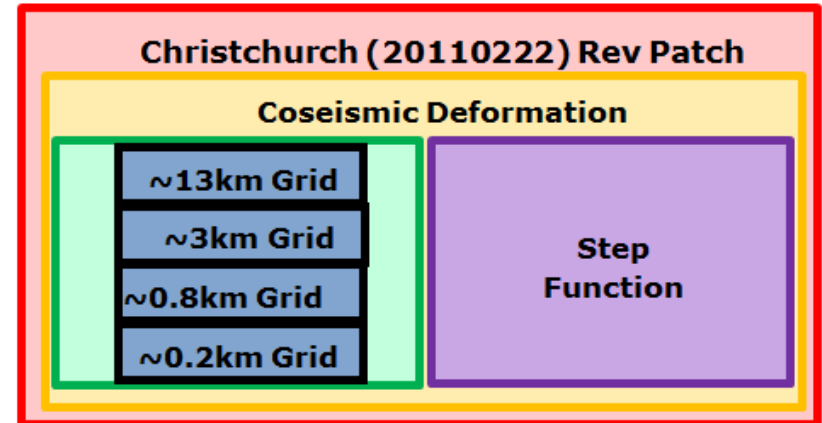
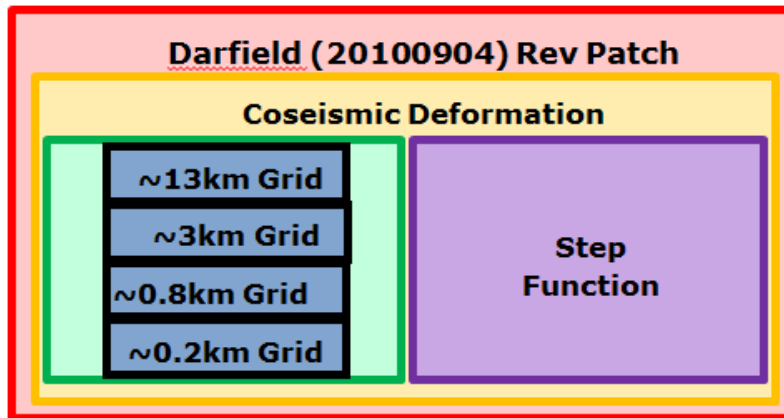
Coseismic Forward Patch and Secular Deformation Model



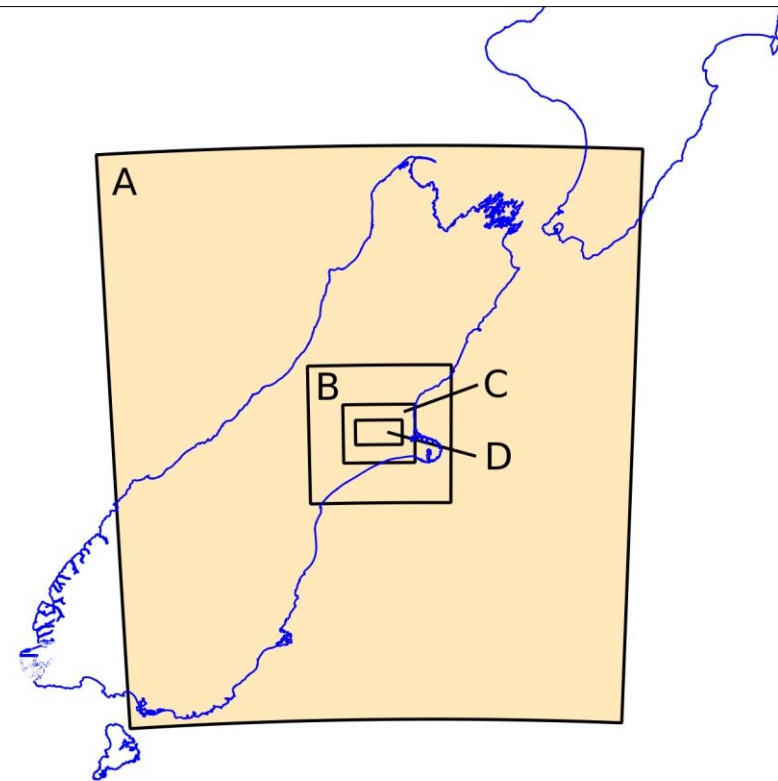
Coseismic Reverse Patch and Secular Deformation Model



Canterbury Earthquakes Submodels



Canterbury Earthquakes Nested Grids

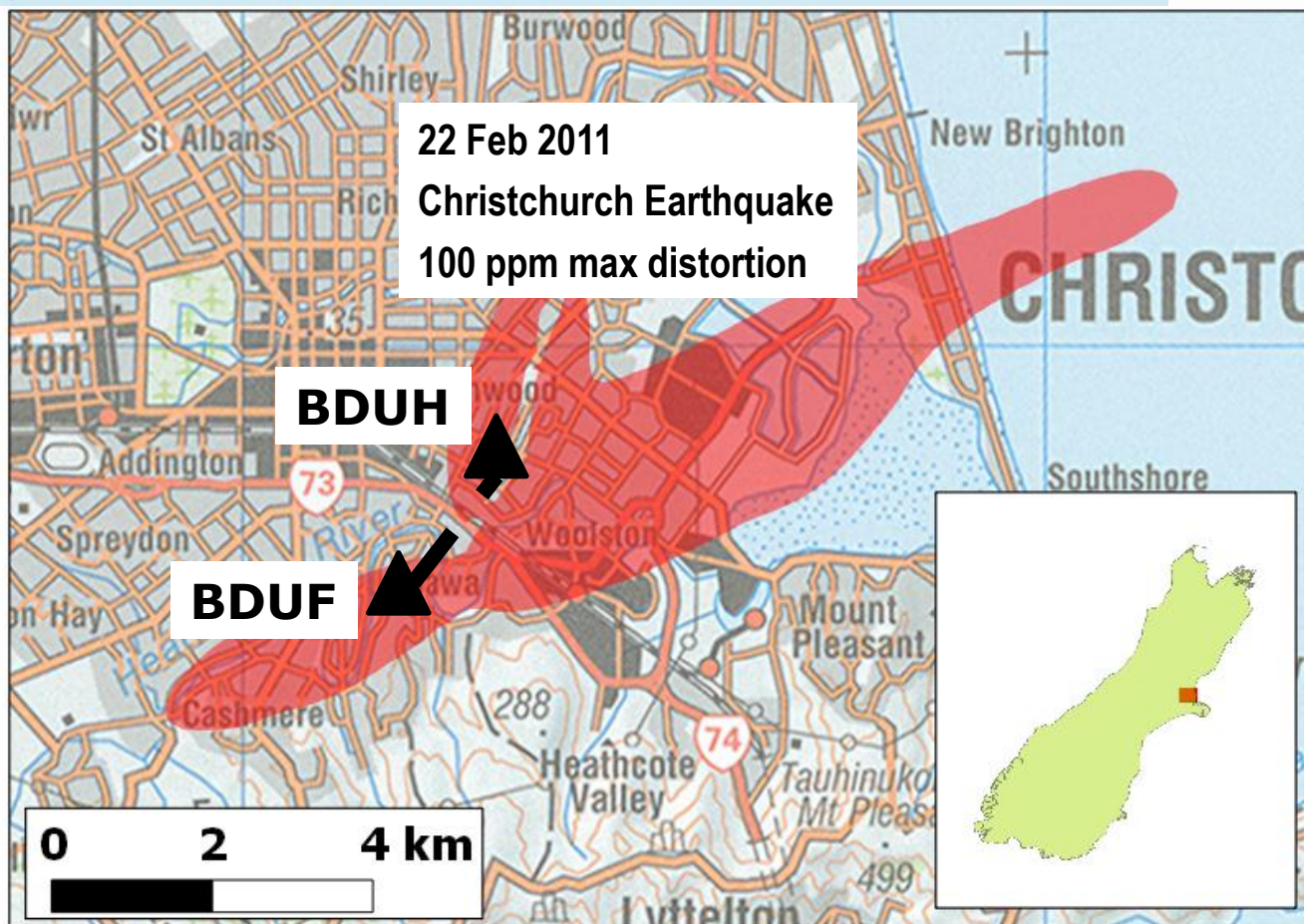


| Grid | No Lon | No Lat | Size Lon (deg) | Size Lat (deg) |
|------|--------|--------|----------------|----------------|
| A | 52 | 54 | 0.15 | 0.125 |
| B | 50 | 59 | 0.075 | 0.0625 |
| C | 84 | 118 | 0.0375 | 0.03125 |
| D | 141 | 306 | 0.01875 | 0.015625 |

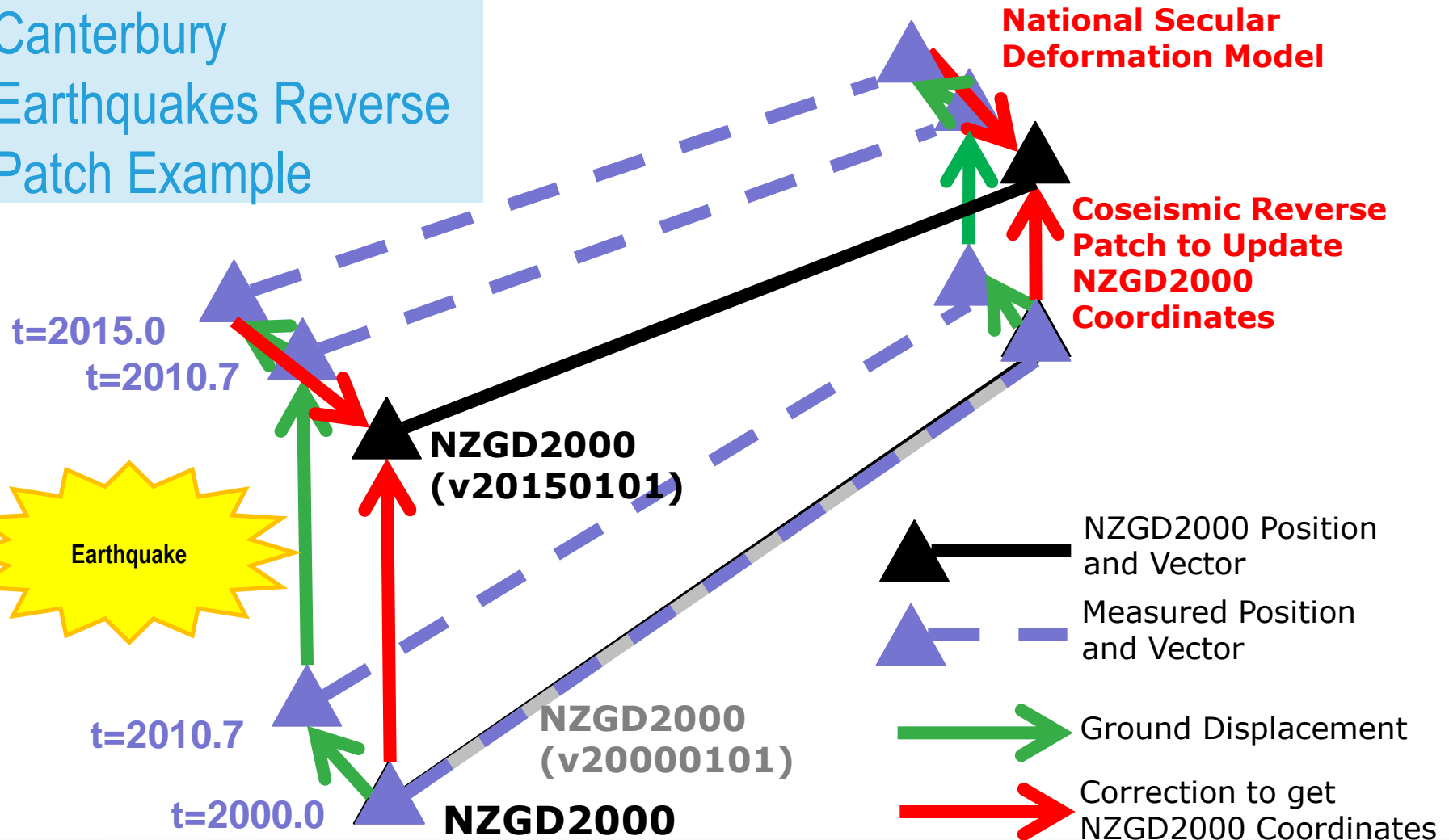


5. Using a Vertical Deformation Model Example

Canterbury Earthquakes Reverse Patch Example



Canterbury
 Earthquakes Reverse
 Patch Example





Deformation Model NOT Used

| From | To | Type | Value | +/- | Calc | +/- | Res |
|------|------|------|----------|-------|----------|-------|---------------|
| | | | X, Y, Z | | X, Y, Z | | E, N, U |
| BDUF | BDUH | GB | -806.601 | 0.016 | -806.611 | 0.000 | 0.003 |
| | | | -660.795 | 0.010 | -660.791 | 0.000 | -0.009 |
| | | | 756.648 | 0.016 | 756.650 | 0.000 | -0.007 |
| | | | 1288.321 | | 1288.326 | | 0.011 |

Deformation Model Used

| From | To | Type | Value | +/- | Calc | +/- | Res |
|------|------|------|----------|-------|----------|-------|---------------|
| | | | X, Y, Z | | X, Y, Z | | E, N, U |
| BDUF | BDUH | GB | -806.601 | 0.016 | -806.611 | 0.000 | 0.003 |
| | | | -660.795 | 0.010 | -660.790 | 0.000 | -0.009 |
| | | | 756.648 | 0.016 | 756.650 | 0.000 | -0.007 |
| | | | 1288.321 | | 1288.327 | | 0.012 |

Reverse Patch with Post-Earthquake Observations



Deformation Model NOT Used

| From | To | Type | Value | +/- | Calc | +/- | Res |
|------|------|------|----------|-------|----------|-------|---------------|
| | | | X, Y, Z | | X, Y, Z | | E, N, U |
| BDUF | BDUH | GB | -806.347 | 0.016 | -806.611 | 0.000 | 0.009 |
| | | | -660.834 | 0.010 | -660.791 | 0.000 | -0.110 |
| | | | 756.753 | 0.016 | 756.650 | 0.000 | -0.265 |
| | | | 1288.244 | | 1288.326 | | 0.287 |

Deformation Model Used

| From | To | Type | Value | +/- | Calc | +/- | Res |
|------|------|------|----------|-------|----------|-------|---------------|
| | | | X, Y, Z | | X, Y, Z | | E, N, U |
| BDUF | BDUH | GB | -806.347 | 0.016 | -806.354 | 0.000 | 0.004 |
| | | | -660.834 | 0.010 | -660.829 | 0.000 | -0.009 |
| | | | 756.753 | 0.016 | 756.758 | 0.000 | -0.002 |
| | | | 1288.244 | | 1288.249 | | 0.010 |

Reverse
 Patch with
 Pre-
 Earthquake
 Observations



Key Points

- User requirements for vertical deformation modelling may differ to horizontal requirements
- A range of observation techniques are required to monitor and model vertical deformation: GNSS, precise levelling, InSAR, LiDAR...
- Vertical deformation models can be incorporated into the local reference frame as either forward or reverse patches
- Reverse patches update heights, which ensures heights continue to represent fluid flow